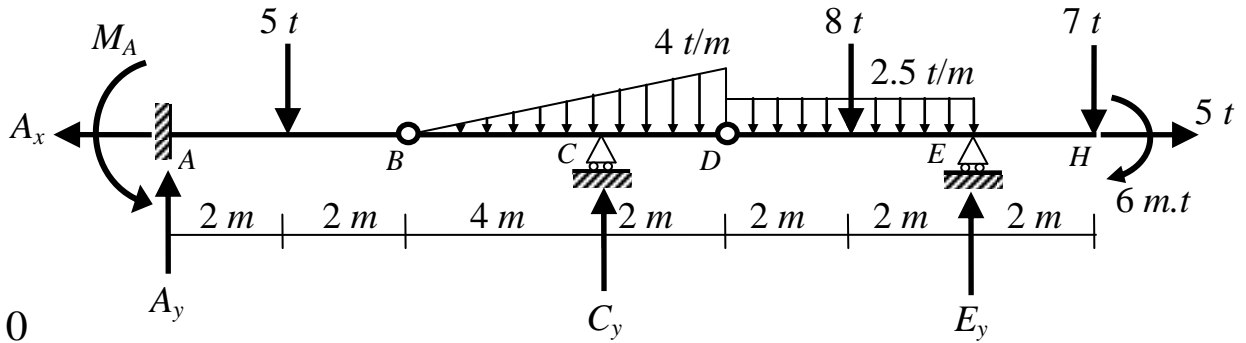


Solution of
First Semester Final Exam

Question (1-a): (10 Marks)

(a) For the shown beam, determine the reactions at the supports A, C and E.

Note: In your answer sheet, draw the final reactions (direction and magnitude) on the beam.



$$+\rightarrow \sum F_x = 0$$

$$-A_x + 5 = 0 \quad \therefore A_x = +5 \leftarrow$$

$$A_x = 5 t \leftarrow$$

$$+\cup \sum_D M_D = 0$$

$$8(2) + 10(2) - E_y(4) + 7(6) + 6 = 0 \rightarrow E_y = 21 t \uparrow$$

$$E_y = 21 t \uparrow$$

$$+\cup \sum_B M_B = 0$$

$$12(4) - C_y(4) + 18(8) - 21(10) + 7(12) + 6 = 0 \rightarrow C_y = 18 t \uparrow$$

$$C_y = 18 t \uparrow$$

$$+\uparrow \sum F_y = 0$$

$$A_y - 5 - 12 + 18 - 18 + 21 - 7 = 0 \rightarrow A_y = 3 t \uparrow$$

$$A_y = 3 t \uparrow$$

$$+\cup \sum_B M_B = 0$$

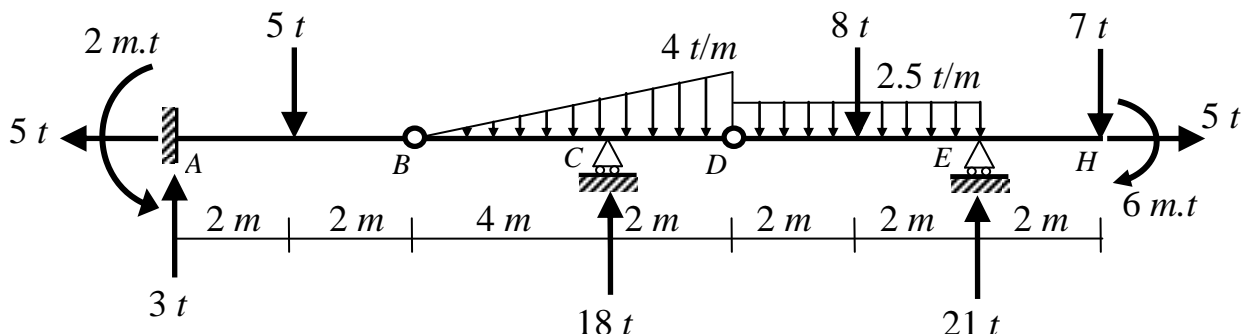
$$3(4) - M_A - 5(2) = 0 \rightarrow M_A = 2 m.t \cup$$

$$M_A = 2 m.t \cup$$

Check:

$$+\cup \sum M_H = 3(16) - 2 - 5(14) + 18(8) - 12(8) - 18(4) + 21(2) + 6 = 0$$

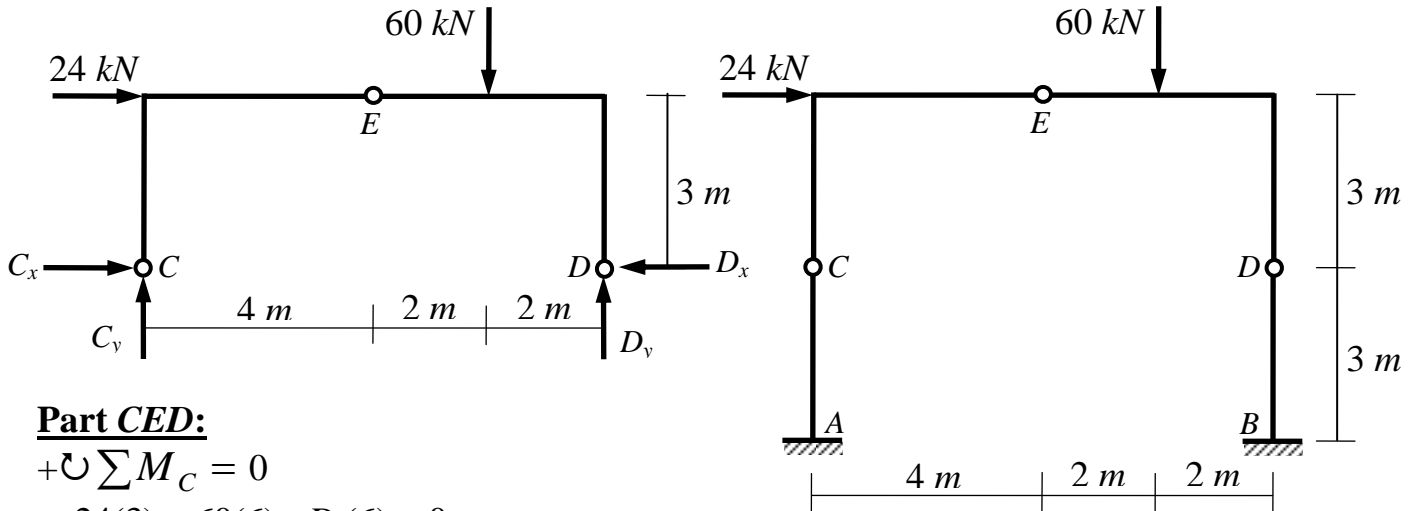
O.K



Question (1-b): (10 Marks)

(b) For the shown frame, determine the reactions at the supports A and B.

Note: In your answer sheet, draw the final reactions (direction and magnitude) on the frame.



Part CED:

$$+\circlearrowleft \sum M_C = 0$$

$$24(3) + 60(6) - D_y(6) = 0$$

$$D_y = 54 \text{ kN } \uparrow$$

$$+\circlearrowleft \sum M_E = 0$$

$$60(2) - D_x(3) - 54(4) = 0$$

$$D_x = 32 \text{ kN } \leftarrow$$

$$+\uparrow \sum F_y = 0$$

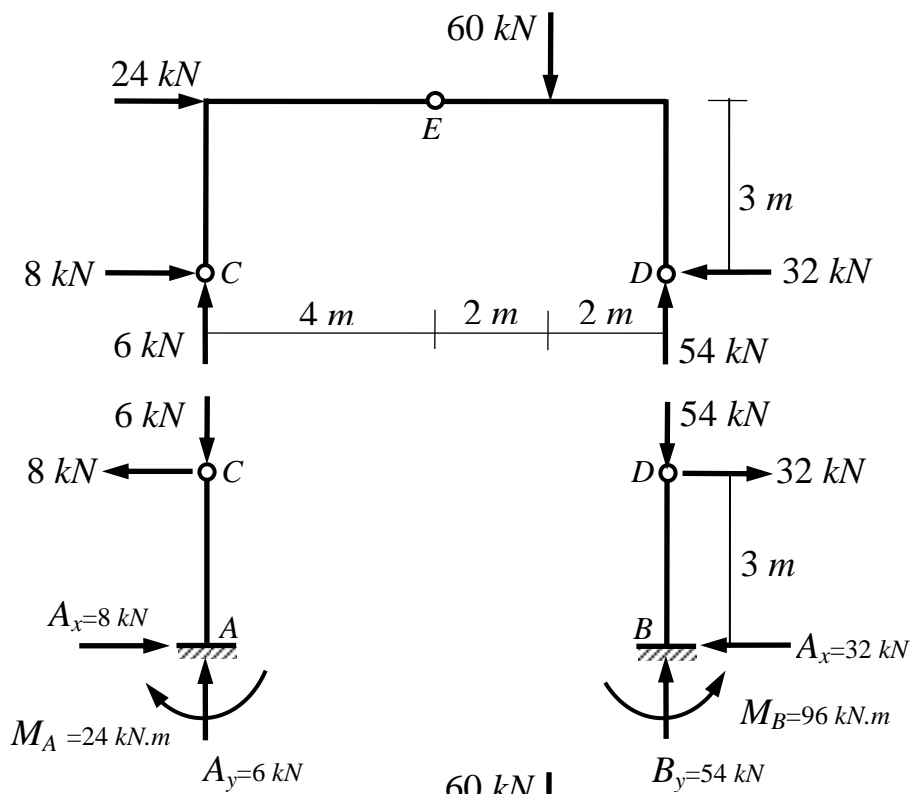
$$C_y - 60 + 54 = 0$$

$$C_y = 6 \text{ kN } \uparrow$$

$$+\rightarrow \sum F_x = 0$$

$$C_x + 24 - 32 = 0$$

$$C_x = 8 \text{ kN } \leftarrow$$



Part AC:

$$A_x = 8 \text{ kN } \rightarrow$$

$$A_y = 6 \text{ kN } \uparrow$$

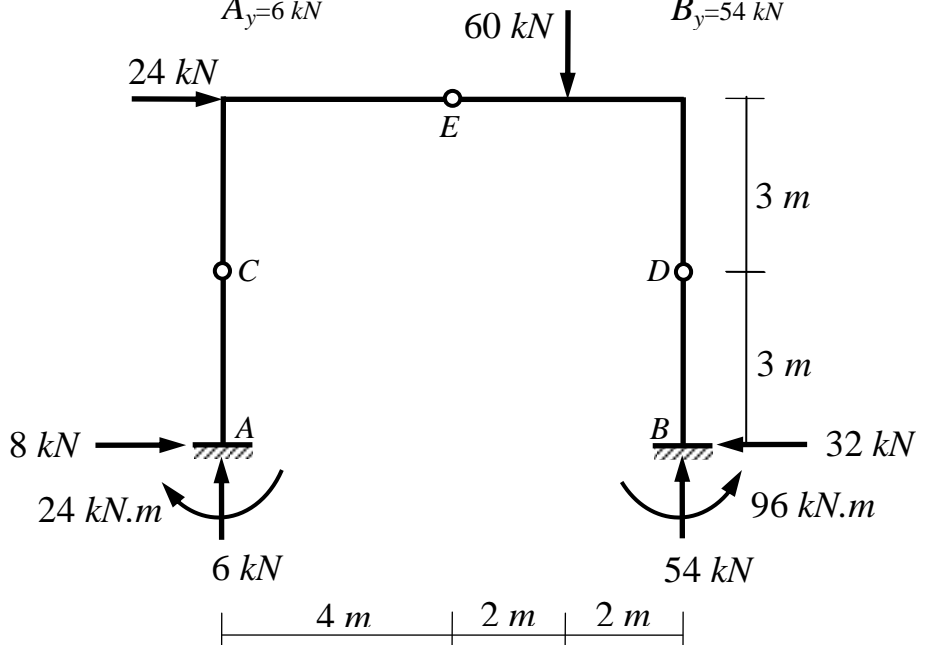
$$M_A = 24 \text{ kN.m } \circlearrowleft$$

Part BD:

$$B_x = 32 \text{ kN } \leftarrow$$

$$B_y = 54 \text{ kN } \uparrow$$

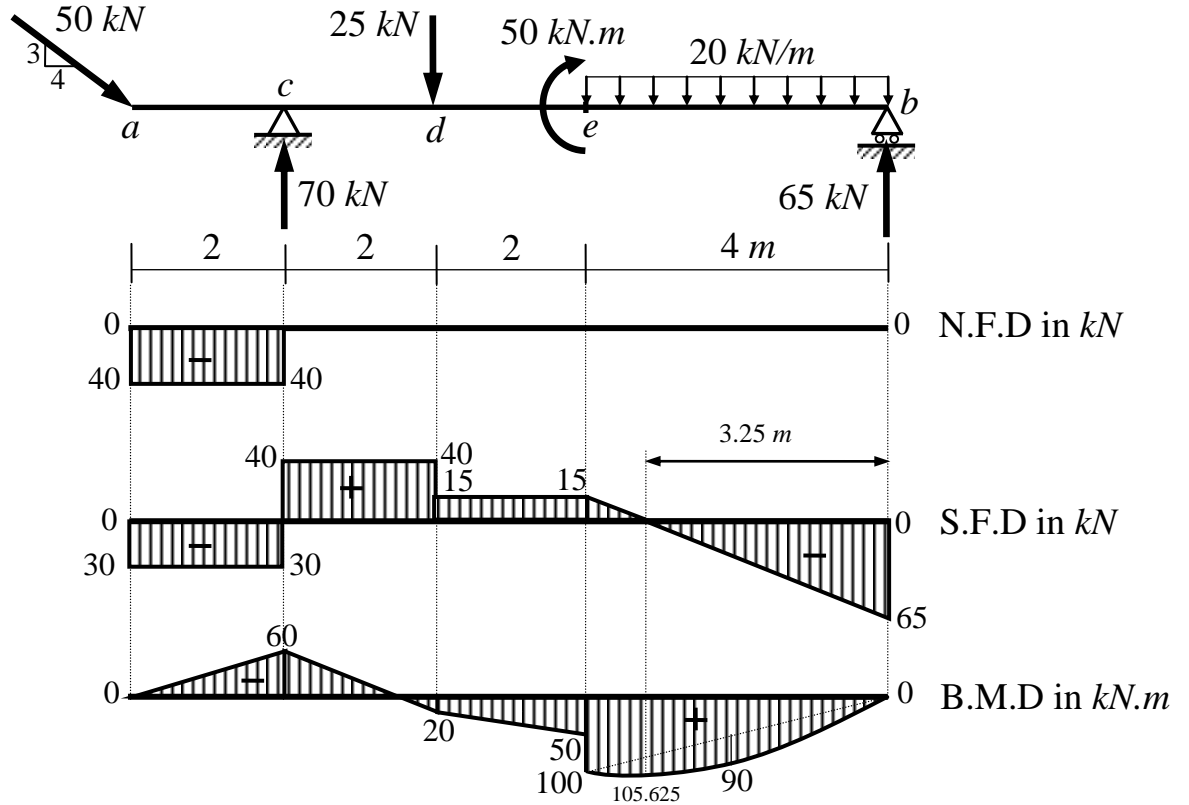
$$M_B = 96 \text{ kN.m } \circlearrowright$$



Question (2-a): (10 Marks)

(a) For the shown beam, draw the normal force, shear force and bending moment diagrams.

Note: Only the vertical reactions are given.

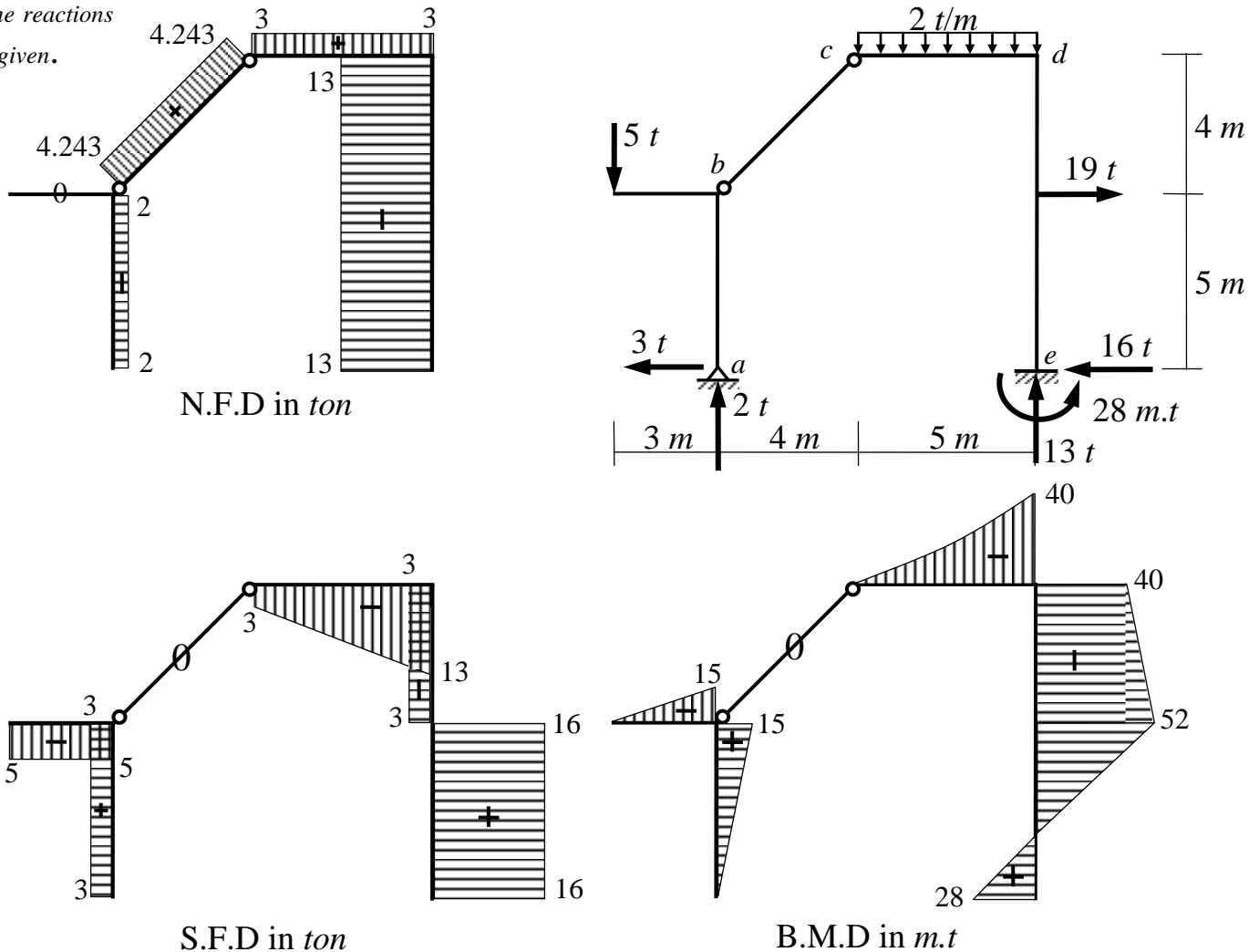


Question (2-b): (10 Marks)

(b) For the shown frame, draw the normal force, shear force and bending moment diagrams.

Note: The reactions are given.

are given.

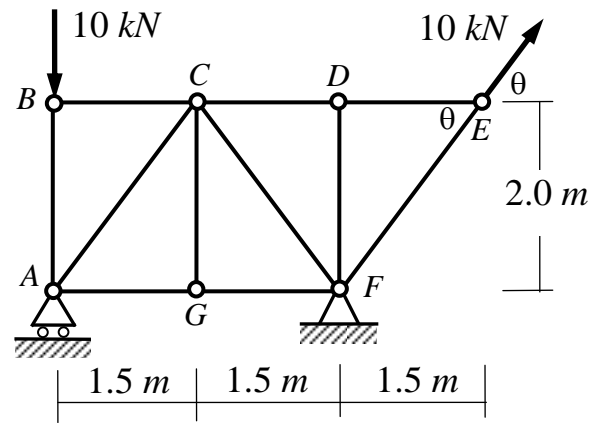


Question (3-a): (11 Marks)

(a) For the shown truss:

- Determine the reactions at the supports A and F.
- Determine the forces in all truss members.
- Using the method of sections, determine the force in member CF.

Note: In your answer sheet, draw the truss and put the force magnitude and the indication (Tension or Compression) on each member.



$$\cos \theta = 1.5/2.5 = 0.6 \quad \sin \theta = 2/2.5 = 0.8$$

$$+\rightarrow \sum F_x = 0$$

$$10 \cos \theta - F_x = 10 \times 0.6 - F_x = 0$$

$$\implies F_x = +6 \text{ kN} \leftarrow \implies \boxed{F_x = 6 \text{ kN} \leftarrow}$$

$$+\uparrow \sum F_y = 0$$

$$F_y + A_y - 10 + 10 \sin \theta = F_y + 10 - 10 + 10 \times 0.8 = 0$$

$$\implies F_y = -8 \text{ kN} \uparrow \implies \boxed{F_y = 8 \text{ kN} \downarrow}$$

(i) The forces in members using the method of joints

Joint B:

$$F_{BA} = 10 \text{ kN (Comp.) and } F_{BC} = 0$$

Joint E:

$$F_{EF} = 10 \text{ kN (Tension) and } F_{ED} = 0$$

Joint D:

$$F_{DF} = 0 \text{ and } F_{DC} = 0$$

Joint A:

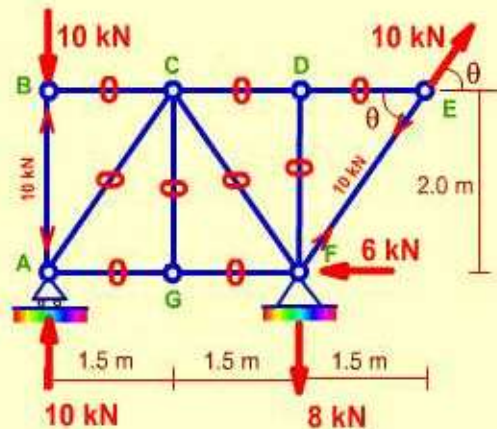
$$F_{AC} = 0 \text{ and } F_{AG} = 0$$

Joint G:

$$F_{GF} = 0 \text{ and } F_{GC} = 0$$

Joint C:

$$F_{CF} = 0$$



(iii) For left Part: $+\uparrow \sum F_y = 0: 10 - 10 - F_{CF} \sin \theta = 0 \implies \boxed{F_{CF} = 0}$

Question (3-b): (9 Marks)

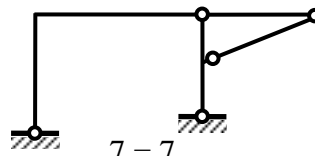
(b) Determine whether each of the shown structures is stable or unstable. If stable, determine whether it is statically determinate or indeterminate.



$$4 = 4$$

Stable + Statically Determinate

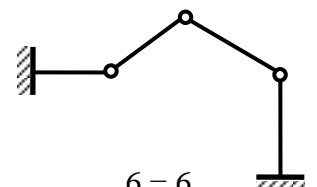
(1)



$$7 = 7$$

Stable + Statically Determinate

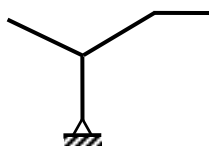
(2)



$$6 = 6$$

Stable + Statically Determinate

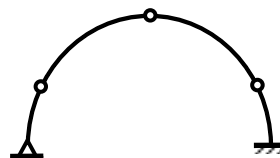
(3)



$$2 < 3$$

Unstable

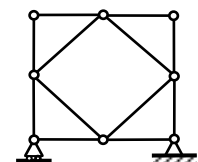
(4)



$$5 < 6$$

Unstable

(5)



$$15 < 16$$

Unstable

(6)

With my best wishes

Dr. M. Abdel-Kader