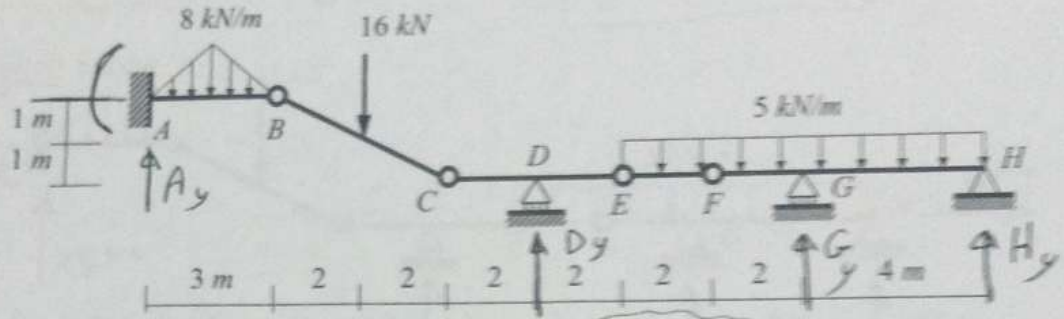


Mid-Term Exam

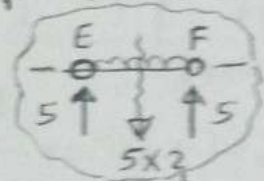
Question (1): (14 Marks)

For the shown beam, determine the reactions at the supports *A*, *D*, *G*, and *H*.
Note: In your answer sheet, draw the final reactions (direction and magnitude) on the beam.



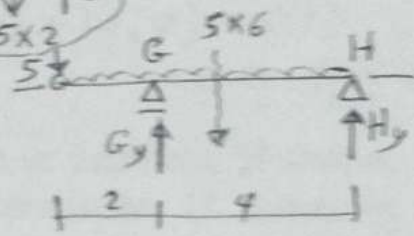
Part EF

$E_y = 5 \text{ kN} \uparrow$ $F_y = 5 \text{ kN} \uparrow$



Part FGH

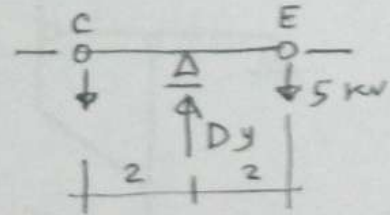
$\sum M_G = 0$
 $-5(2) + (5 \times 6)(1) - H_y(4) = 0$
 $\therefore H_y = 5 \text{ kN} \uparrow$



$\sum F_y = 0$ $-5 + G_y - 5 \times 6 + 5 = 0 \Rightarrow G_y = 30 \text{ kN} \uparrow$

Part CDE

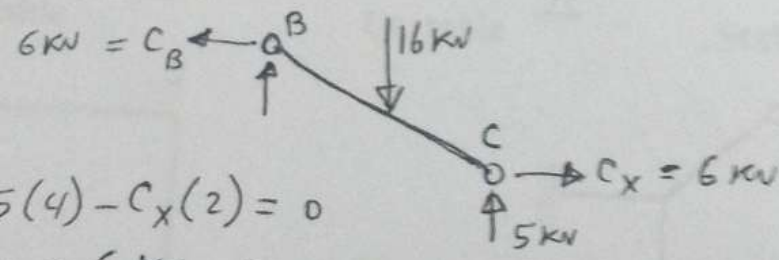
$\sum M_c = 0$ $-D_y(2) + 5(4) = 0$
 $\therefore D_y = 10 \text{ kN} \uparrow$



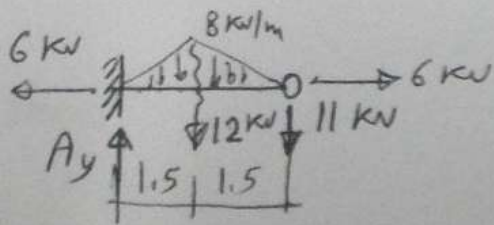
$\sum F_y = 0$ $C_y - 10 - 5 = 0 \Rightarrow C_y = 5 \text{ kN} \downarrow$

Part BC

$\sum M_B = 0$
 $16(2) - 5(4) - C_x(2) = 0$
 $\Rightarrow C_x = 6 \text{ kN} \rightarrow$
 $\Rightarrow C_B = 6 \text{ kN} \leftarrow$
 $\sum F_y = 0 \Rightarrow B_y = 11 \text{ kN} \uparrow$



Part AB



Part AB (Continue)

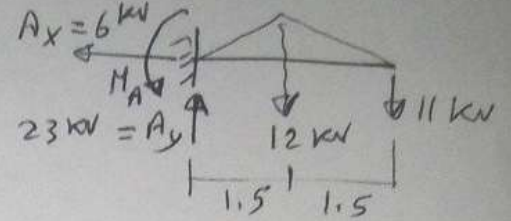
$$+\uparrow \sum F_y = 0 \quad A_y - 12 - 11 = 0 \Rightarrow A_y = 23 \text{ kN } \uparrow$$

$$+\rightarrow \sum F_x = 0 \Rightarrow A_x = 6 \text{ kN } \leftarrow$$

$$+\circlearrowleft \sum M_A = 0 \quad -M_A + 12(1.5) + 11(3) = 0$$

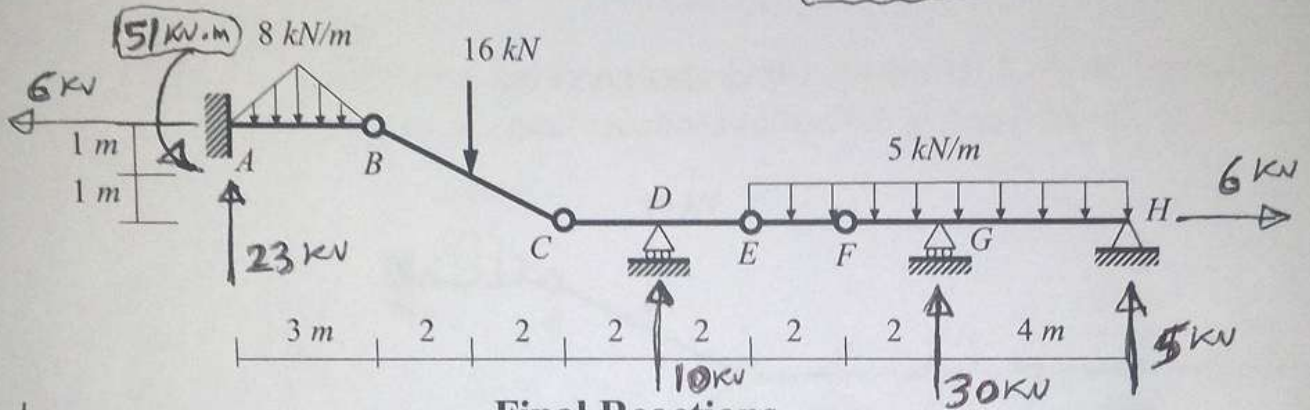
$$\therefore M_A = 51 \text{ kN}\cdot\text{m } \curvearrowleft$$

$$A_y = 23 \text{ kN } \uparrow$$



For the entire beam

$$\sum F_x = 0 \Rightarrow H_x = 6 \text{ kN } \rightarrow$$



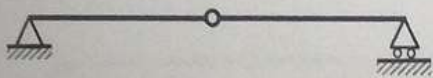
Final Reactions

Check:

$$+\circlearrowleft \sum M_H = -51 + 23(19) - 16(14) + 10(10) - 40(4) + 30(4) - 6(2) - 12(17.5) = 0 \text{ O.K. } \checkmark$$

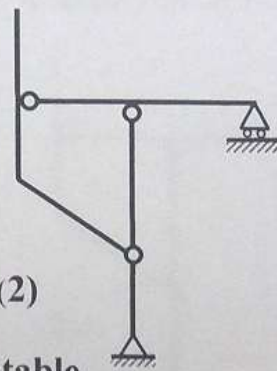
Question (2): (6 Marks)

Determine whether each of the shown structures is stable or unstable. If stable, determine whether it is statically determinate or indeterminate. If statically indeterminate, determine the degree of indeterminacy.



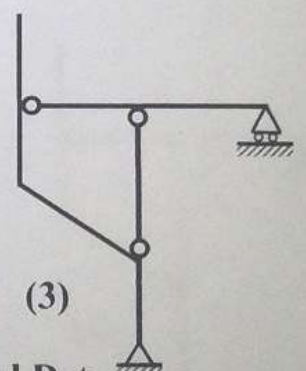
(1)

Unstable



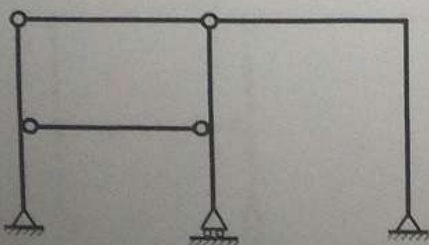
(2)

Unstable



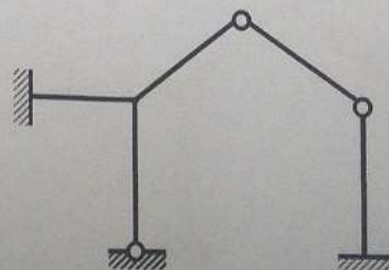
(3)

Stable and Det.



(4)

Stable and Det.



(5)

Statically Indeterminate to the third degree